

# **FORM TP 2023020**

**JANUARY 2023** 

#### CARIBBEAN EXAMINATIONS COUNCIL

# CARIBBEAN SECONDARY EDUCATION CERTIFICATE® EXAMINATION

#### **MATHEMATICS**

#### Paper 02 – General Proficiency

#### 2 hours 40 minutes

#### READ THE FOLLOWING INSTRUCTIONS CAREFULLY.

- 1. This paper consists of TWO sections: I and II.
- 2. Section I has SEVEN questions and Section II has THREE questions.
- 3. Answer ALL questions.
- 4. Write your answers in the spaces provided in this booklet.
- 5. Do NOT write in the margins.
- 6. All working MUST be clearly shown.
- 7. A list of formulae is provided on page 4 of this booklet.
- 8. If you need to rewrite any answer and there is not enough space to do so on the original page, you must use the extra page(s) provided at the back of this booklet. Remember to draw a line through your original answer.
- 9. If you use the extra page(s), you MUST write the question number clearly in the box provided at the top of the extra page(s) and, where relevant, include the question part beside the answer.
- 10. ALL diagrams in this booklet are NOT drawn to scale, unless otherwise stated.

#### **Required Examination Materials**

Electronic calculator Geometry set

# DO NOT TURN THIS PAGE UNTIL YOU ARE TOLD TO DO SO.

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#### LIST OF FORMULAE

V = Ah where A is the area of a cross-section and h is the perpendicular Volume of a prism length.

 $V = \pi r^2 h$  where r is the radius of the base and h is the perpendicular height. Volume of a cylinder

 $V = \frac{1}{3}Ah$  where A is the area of the base and h is the perpendicular height. Volume of a right pyramid

 $C = 2\pi r$  where r is the radius of the circle. Circumference

 $S = \frac{\theta}{360} \times 2\pi r$  where  $\theta$  is the angle subtended by the arc, measured in Arc length degrees.

 $A = \pi r^2$  where r is the radius of the circle. Area of a circle

 $A = \frac{\theta}{360} \times \pi r^2$  where  $\theta$  is the angle of the sector, measured in degrees. Area of a sector

 $A = \frac{1}{2}(a+b)h$  where a and b are the lengths of the parallel sides and h Area of a trapezium is the perpendicular distance between the parallel sides.

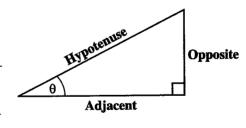
If  $ax^2 + bx + c = 0$ , Roots of quadratic equations

then 
$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

 $\sin \theta = \frac{\text{length of opposite side}}{\text{length of hypotenuse}}$ Trigonometric ratios

 $\cos \theta = \frac{\text{length of adjacent side}}{\text{length of hypotenuse}}$ 

 $\tan \theta = \frac{\text{length of opposite side}}{\text{length of adjacent side}}$ 



Area of a triangle

Sine rule

Area of  $\Delta = \frac{1}{2}bh$  where b is the length of the base and h is the perpendicular height.

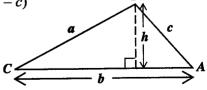
Area of 
$$\triangle ABC = \frac{1}{2}ab \sin C$$

Area of  $\triangle ABC = \sqrt{s(s-a)(s-b)(s-c)}$ 

where  $s = \frac{a+b+c}{2}$ 

 $\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$ 

 $a^2 = b^2 + c^2 - 2bc \cos A$ Cosine rule



#### **SECTION I**

# Answer ALL questions.

# All working must be clearly shown.

1. (a) (i) By rounding each number in the expression below to one significant figure, estimate the value of

$$\frac{\sqrt{108}}{19.72 + 5.296}$$

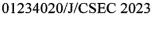
(2 marks)

(ii) Find the EXACT value of

$$3\frac{3}{8} \div \left(\frac{5}{12} + \frac{1}{3}\right).$$

Give your answer as a mixed number in its simplest form.

(3 marks)





Due to the COVID-19 pandemic, the number of available seats in a hall was reduced from (b) 125 to 93. Calculate the percentage decrease in the number of available seats.

(2 marks)

Mica invests a certain amount of money in a bank that pays compound interest at a rate (c) of 2.5% per annum. At the end of 2 years, the value of her investment is \$7 564.50.

Calculate the amount Mica invests.

Compound interest: 
$$A = P\left(1 + \frac{r}{100}\right)^n$$
, where,  $A = \text{total amount after } n \text{ years};$ 

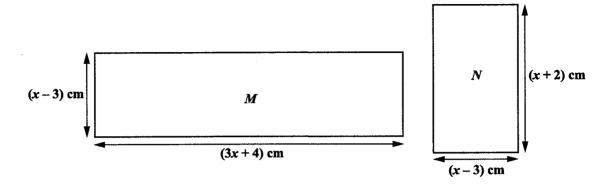
P = principal or original value;

r = rate of interest per annum; n = number of years the money is invested

(2 marks)

				Page 7
2.	(a)	Simp	lify:	
		(i)	$\left(x^3\right)^2$	
		(ii)	$y^8 \div y^{-5}$	(1 mark)
	(b)	(i)	Factorize:  a) $xy - y^2$	(1 mark)
				(1 mark)
			b) $x^2 - y^2$	
				(1 mark)
		(ii)	Hence, simplify the expression $\frac{xy - y^2}{x^2 - y^2}.$	
				(1 mark)

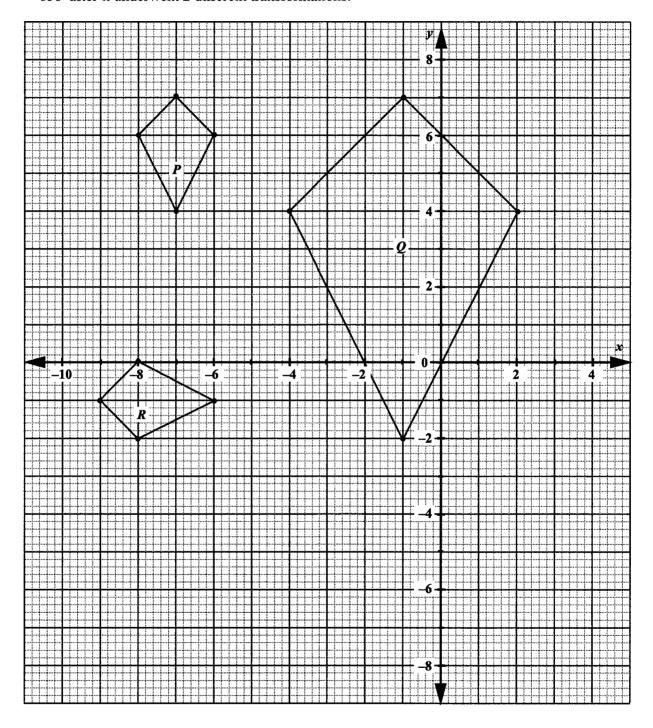
(c) The diagram below shows 2 rectangles, M and N, with their dimensions expressed in terms of x.



Given that the difference between the areas of the two rectangles is 64 cm<sup>2</sup>, show that  $x^2 - 2x - 35 = 0$ .

(4 marks)

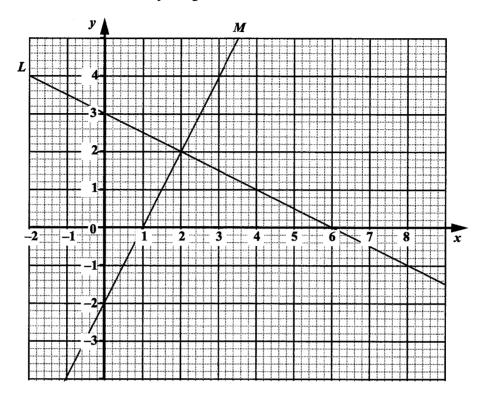
3. The following diagram shows 3 quadrilaterals, P, Q and R on a square grid. Q and R are the images of P after it underwent 2 different transformations.





(a)	On th	ne grid <b>on page 9</b> , draw the image of quadrilateral P after a	
	(i)	translation by the vector $\begin{pmatrix} 10 \\ -4 \end{pmatrix}$ . Label this image $P'$	(1 mark)
	(ii)	reflection in the line $y = 0$ . Label this image $p''$ .	(2 marks)
(b)	Desc	ribe fully a single transformation that maps Quadrilateral P onto	
	(i)	Quadrilateral $Q$	
			••••••
			•••••
			•••••
			•••••
			(3 marks)
	(ii)	Quadrilateral R.	
			•••••
			•••••
			••••••
			(3 marks)

4. Lines L and M are drawn on the square grid below.



- (a) Write down the coordinates of the
  - (i) x-intercept of Line L

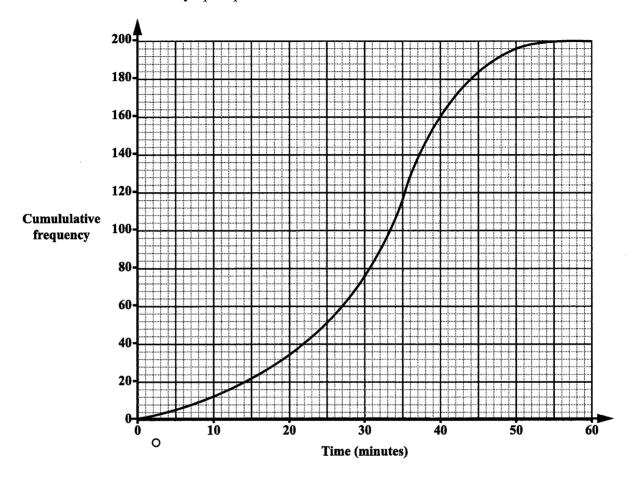
(1 mark)

(ii) y-intercept of Line M.

(1 mark)

(b)	The equation of Line L is $x + 2y - 6 = 0$ . Find the value of k given that the lies on Line L.	point (9, <i>k</i> )
		(2 marks)
(c)	Find the equation of Line $M$ , in the form $y = mx + c$ .	
		(2 marks)
(d)	Show by calculation, that Line $L$ and Line $M$ are perpendicular.	
		(2 marks)
(e)	Line $L$ and Line $M$ represent the graph of a pair of simultaneous equations. graph on page 11, write down the solution to the pair of simultaneous equation	
	······································	(1 mark)

5. The cumulative frequency curve below shows information about the times taken by 200 students to solve a Mathematics Olympiad problem.



(a) Using the cumulative frequency curve shown above, find an estimate for the

		(1 mark)
(i)	number of students who took more than 50 minutes to solve the p	roblem

(ii) median time taken to solve the problem

	(1 mark)

|--|--|--|--|--|--|--|

(b) (i) Using the cumulative frequency curve on page 13, complete the table below.

Time (minutes)	Midpoint (x)	Frequency (f)	Frequency × Midpoint (fx)
1 – 10	5.5	12	66
11 – 20	15.5		
21 – 30	25.5	42	1071
31 - 40	35.5	84	2982
41 – 50	45.5		
51 – 60	55.5	4	222

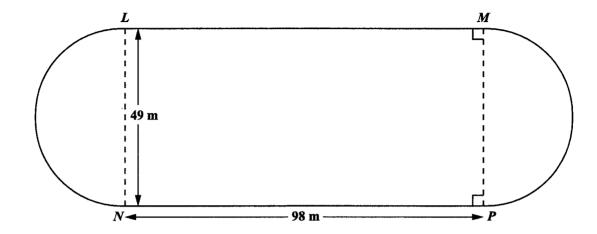
(3 marks)

(ii) Use the information in the completed table above to calculate an estimate of the average time taken by the students to solve the problem.

(2 marks)

In this question, use  $\pi = \frac{22}{7}$ . 6.

> The diagram below shows a scaled drawing of a running track. It consists of a rectangle and two semicircles with diameters LN and MP. LN = MP = 49 m and LM = NP = 98 m.



Show that the TOTAL length of the running track is 350 m. (a) (i)

(2 marks)



	(ii)	Nathan walks at a constant rate of 1.4 m/s. Calculate the time it will take him to walk 7 laps around the track.
		(2 marks)
(b)	Tafari	runs one lap of the track in 68 seconds.
	(i)	Determine the number of laps Tafari can complete in one hour, running at the same speed.
		(2 marks
	(** <u>)</u>	·
	(ii)	Nathan completes running one lap of the track every 72 seconds. Tafari and Nathan start running at the same time from point $L$ on the track. Each complete a number of laps of the track. Calculate the LEAST number of laps that each will complete before they are both at point $L$ again at the same time.
		TI C : 1.4 long at NI-there are walked as long
		Tafari completes laps and Nathan completes laps.  (3 marks)

7. The grid below shows the first 3 figures in a sequence. Each figure is made using a set of small squares of unit length that are **both** coloured (shaded) and white (unshaded).

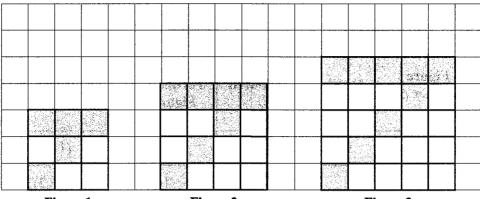


Figure 1

Figure 2

Figure 3

(a) In the space provided below, draw Figure 4 of the sequence.

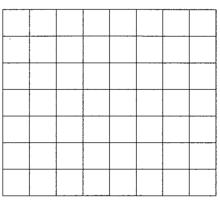


Figure 4

(2 marks)



(b) The number of coloured squares, C, the total number of squares, T and the perimeter of the figure, P, follow a pattern. Study the patterns in the table below and answer the questions that follow.

Complete Rows (i), (ii) and (iii) in the table below.

	Figure Number (F)	Number of Coloured Squares (C)	Perimeter of Figure (P)	Total Number of Squares (T)	
	1	5	12	$(1+2)^2 = 9$	
	2	7	16	$(2+2)^2 = 16$	<del>-</del>
	3	9	20	$(3+2)^2 = 25$	
	:	:	:	:	
(i)	11		52		(2 marks)
	:	:	:	:	
(ii)		49		$(23+2)^2 = 625$	(2 marks)
	:	:	:	:	
(iii)	n				(3 marks)

(c) How many white squares are in Figure 11.

•••••••••••••••••••••••••••••••••••••••	
(1 mark)	

**Total 10** marks

#### **SECTION II**

# Answer ALL questions.

# ALGEBRA, RELATIONS, FUNCTIONS AND GRAPHS

8.	The t	functions	f, o	and h are	e defined	as follows:
0.	1110	luncuons	ノッ ろ	und / unv		as ionoms.

$$f(x) = 4x - 1$$
,  $g(x) = x^2 - 5$  and  $h(x) = 3^x$ .

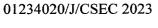
- (a) Find
  - (i) g(x-2), in its simplest form

(ii)  $f^{-1}(11)$ 

(2 marks)

(b) Determine the value of hh(1).

(2 marks)



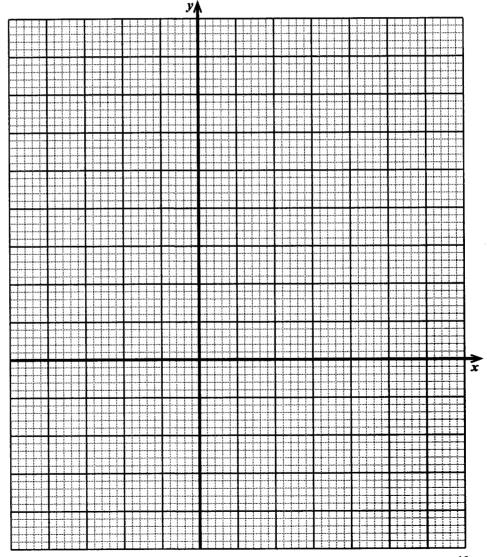


The function f is defined as follows: (c)

$$f: x \to x^2 - x - 2.$$

Complete the table below and plot the graph for the function  $f(x) = x^2 - x - 2$  on the grid that follows.
(Use a scale of 2 cm to represent 1 unit on both axes.)

х	-2	-1	0	1	2	3
f(x)		0	<u></u>	-2	0	4

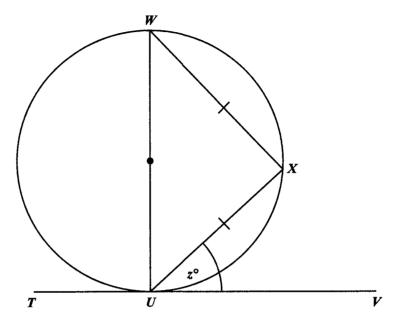


(6 marks)

**Total 12 marks** 

#### **GEOMETRY AND TRIGONOMETRY**

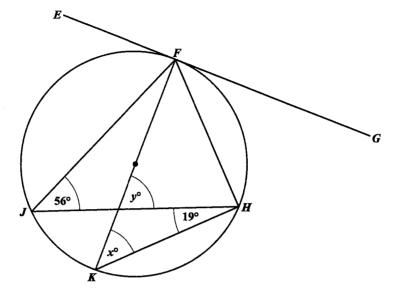
9. (a) W, X and U are points on the circumference of a circle. TV is a tangent to the circle at U. UW is a diameter of the circle and triangle WXU is isosceles.



Using appropriate theorems, state THREE reasons that explain why the measure of Angle z is 45°.

Reason 1	
Reason 2	
Reason 3	
	(3 marks)

(b) The diagram below shows a circle with diameter KF. Line EFG is a tangent to the circle at F. The points F, H, K and J lie on the circumference of the circle.



By showing EACH step in your work, where appropriate, find the value for EACH of the following angles:

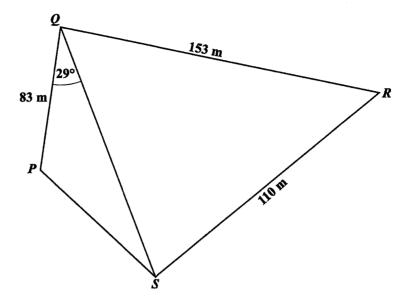
(i)	Angla	v
(1)	Angle	х

 •••••
(1 mark)

(ii) Angle y.

(2 marks)

(c) The diagram below shows 4 points, P, Q, R and S on level ground, where pillars will be placed to mark the outline for a foundation.



(i) There is a vertical post, RT, at R. From Q, the angle of elevation of the top of the post, T, is 21°. Find the height of the post.

(2 marks)

(ii)	Given that the length $QS$ is 135 m, calculate the perimeter of the foundation $PQRS$ .
	(4 marks)
	(4 marks)
	Total 12 marks
	Iviai 12 marks

#### **VECTORS AND MATRICES**

10. (a) Three matrices Q, R and S are as follows:

$$Q = \begin{pmatrix} 2 & -1 \\ 4 & 3 \end{pmatrix}, R = \begin{pmatrix} 1 & 6 \\ -5 & 4 \end{pmatrix}, S = \begin{pmatrix} 2 & 7 \\ 4 & -1 \\ -8 & 9 \end{pmatrix}.$$

Calculate the matrix product QR.

(i)	Explain why the matrix product QS is NOT possible.	
		(1 mark)
(ii)	State the order of the matrix product SR.	
		(1 mark)

(2 marks)

GO ON TO THE NEXT PAGE



(iii)



Given that  $A = \begin{pmatrix} 4 & -1 \\ -7 & x \end{pmatrix}$ , determine the value of x when |A| = 5. (b)

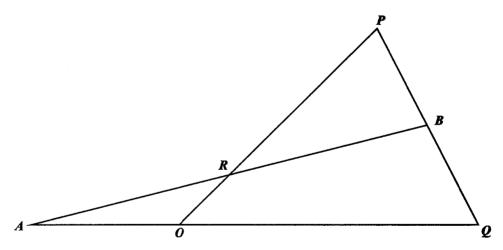
(2 marks)

In the diagram below, OPQ is a triangle. ARB and AOQ are straight lines. (c) B is the midpoint of PQ.

R is the midpoint of AB.

$$OR : RP = 1 : 3.$$

$$\overrightarrow{OP} = 4\mathbf{a}$$
 and  $\overrightarrow{OQ} = 8\mathbf{b}$ .



Find, in terms of a and/or b, in its simplest form

(i) 
$$\overrightarrow{PQ}$$

(1 mark)

(ii)	$\overrightarrow{PR}$	
		(2 marks)
iii)	$\overrightarrow{RB}$ .	
,		
		(3 marks)
		Total 12 maulza

# **END OF TEST**

IF YOU FINISH BEFORE TIME IS CALLED, CHECK YOUR WORK ON THIS TEST.

